A superpopulation model... Z; 2 Treatment naicotor Tico), Till) = Potential authoris. We usually assume that we observe i.i.d. samples. (Zi, Tivi, Yi), Xi) drawn fran a superpopulation. [i.e. a density over (2, yw), yor, x).]. The average treatment offut (ATE) is now an experistion: ~ = E[XU] - E[XO]]. What goes enoug? We obser only Excell and Excellz=0]. In general, there are different from E[160] and E[260] respectively. Se - the prima freie treatment effect defind Top = P[tu]/Z=1] - E[tu]/Zeo] is not the same as T. Can unit t as T = E[YU)] - E[YW)] = P[xu) | Z=1]. P(Z=1) + P[xu) | Z=0]. P(Z=0) -(E[YW1Z=1]P(Z=1) + E[YW)1Z=Q-P(Z=0).)

We do not observe the highlighted terms, so T

is not Identifiable unless we make further assumptions
What does vandourrection give us?
Z # {4 w), 4 co)}.
Kemi This is not saying that 211 day.
). This implies. E[Yu) Z = 1] = E[Yu) Z = 0].
=) P[Y(1)] = P[Y(1)12=]. Analogously, P[Y(0)] = P[Y(0)1Z=0].
2). T = TPF
as to identify ATE in observational studies.
Unionformdedries. 1 ignorbility lexchangeability:
(74), 760)] 1 Z X
Defu The = EYU) X=x].
TARLA) = E[YU) X=x, Z=1] - E[YU) X=x, Z=0].
Il unionformdednes holds, then.
FLYU) 12=0, X=x] = FLYU) [X=x].
=) T(x) = Tpp(x).

If. X & disuite, then.

When X is cts, or X has many leads, then need aturn methods...

3 methods: O Regression.

3 Matching.

Buck to bidney stones.

-	Treatment A helps.	Tratment B helps.
Large bidney stores.	69°6	73%
Small bilaney	872	93%.
All patients	837	78%

Inoportion of partients = 51%

$$T(1) = E[YU][X=1] - E[YO][X=1].$$

$$= E[YU][X=1, Z=1] - E[YO][X=1, 2=0].$$

$$= 0.98 - 0.87$$

$$= 0.06.$$

= 0,04

 $T = \tau(1) \cdot P(X=1) + \tau(0) \cdot P(X=0)$ = 0.06 \cdot 0.51 + 0.04 \cdot 0.49. \(\pi \ 0.05\).

Methods for estimating ATE under unconfoundedness.

Mothod 1: Outcome regression.

ATE $\tau = \mathbb{E}[\tau(X)] = \int \tau(x) \cdot p(x) dx$.

when $p(x) = \text{density of } X_{x}$ and. $\tau(x) = \mathbb{E}[Y(x)|X=x] - \mathbb{E}[Y(x)|X=x]$.

is called the Coorditional Army Treatment Effect.

(CATE), function.

Outune regression comprises 2 steps:

Seep 1: Estmose Clx) viz Elx).

Step 2: Un plug in estimator for T. Ci.e. we substitute p(p) with empirical distribution of [2/1,-, Xn]].

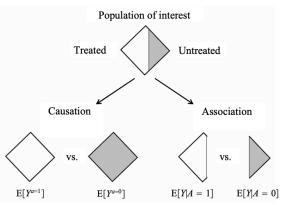
Henry 2 = 1 7 2(Xi).

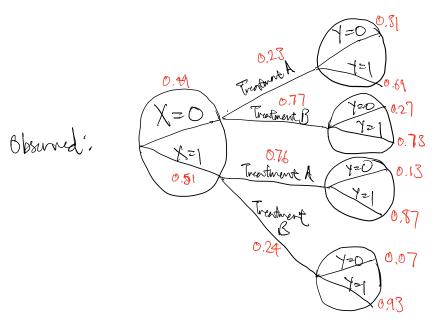
To estmete T is tricky,

Many soretegies, we will starte 2 of these.

Strottegy 1: Fif joint model for Mx, 2) = [[1]obs | X=x, Z=z]
observe that the the thing who, 1) - who, 0).

Strategy 2: Fix 2 models, one each for · May (20) = P[You | X=x, Z=] · Ma, 6) = P[Yoks K=x, Z=0]. Observe that the the)= Mus (x) - Mas (x). What can we use to estimate on, men mos? · Lnear model. Y Model may la misspreified · ML mothods. > problems with overfitting Fact: Use Strategy I with a linear model, i.e. regress 1 ~ X+Z, get is a model. Y= 2+157x+12+E. Then 2=8. Pf. Elx). = Mla1)-Mu,0)- [My,2)= 2+ BTx+82] 三 分. 一一个一个. 图 Method. 2! Inverse proposity score weighting





See slides/levent video for expansition of above.

Thur. Assume ?[0], Yw) & 12/X., then.

2
$$\mathbb{E}\left[\frac{\int_{obs}C_1-Z_1}{1-e(x)}\right] = \mathbb{E}\left[\frac{1}{1}\cos\left(\frac{1}{1}\right)\right]$$

Hence, $\tau = \mathbb{E}\left[\frac{1}{\log 2} - \mathbb{E}\left[\frac{1}{1-\log 2}\right]\right]$

For finite sample, he have the inverse proposity weighting (IBW) estimator.

When Elos is an estender of els.

Fact. Assume. 3[0], Yw) 342[X; then.

Proofs of Thur, Fact are easy.