

1. Frame each scenario as a multi-armed bandits problem. Describe in words what the arms and the payoffs are.
    - (a) You're trying to figure out which restaurant on Euclid is your favorite, so every day for a month you get lunch at one of the restaurants on Euclid.
  
  
  
  
  
  
  
  
  
  
    - (b) You're trying to figure out what time of day your shower is most likely to have warm water, so you take a shower at a different time of day for a sequence of days and observe the temperature of the water.
  
  
  
  
  
  
  
  
  
  
  2. (a) Let  $X_1, \dots, X_n$  be i.i.d. random variables with variance  $\sigma^2$ , mean  $\mu$ , and let  $Z = \frac{1}{n} \sum_{i=1}^n X_i$ . What is  $\text{Var}(Z)$ ?
  
  
  
  
  
  
  
  
  
  
  - (b) Using Chebyshev's inequality, find an upper bound on the probability that  $Z$  is at least  $\epsilon$ -far away from  $\mu$ , i.e. on  $\mathbb{P}[|Z - \mu| \geq \epsilon]$ .
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3. Suppose you're trying to find the fastest driving route from Berkeley to San Francisco at 8 am out of 3 different routes. To try to determine this, every day for 5 days you drive from Berkeley to San Francisco at 8 am, choosing one of the routes each day.



4. Let  $X$  be the sum of 20 i.i.d. Poisson random variables  $X_1, \dots, X_{20}$  with  $\mathbb{E}[X_1] = 1$ . Use the following techniques to upper bound  $\Pr(X \geq 26)$ .

- (a) Markov's Inequality
- (b) Chebyshev's Inequality
- (c) Chernoff Bound

Hint 1: The MGF of a mean- $\lambda$  Poisson random variable  $X$  is

$$M_X(t) = e^{\lambda(e^t - 1)}.$$

Hint 2: if  $X, Y$  are independent Poisson random variables with parameter  $\lambda_1, \lambda_2$ , then  $Z = X + Y$  is a Poisson random variable with parameter  $\lambda_1 + \lambda_2$ .

## Feedback Form

On a scale of 1-5, where 1 = much too slow and 5 = much too fast, how was the pace of the discussion section?

1 2 3 4 5

Which problem(s) did you find most useful?

Which were least useful?

Any other feedback?